

MASTER IN ARTIFICIAL INTELLIGENCE (UDC - USC - UVigo)  
REASONING AND PLANNING exam. June 17th, 2024

Surname: \_\_\_\_\_

First Name: \_\_\_\_\_

**INSTRUCTIONS** This exam covers units 1-6 and is weighted with a maximum of **42 points (pt)** from a total of **100 pt** in the whole course (Unit 7 is not covered in the exam and weights 8 pt). For the test, use the original statement sheet and avoid corrections or unclear marking (ask for a new blank sheet if needed). **Completion time = 2 hours.**

— EXAM —

**Exercise 1 (20pt).** Each question has at least one correct answer and its total score depends on whether you check: some incorrect answer = **-3pt**; all the correct answers = **5pt**; only correct answers, but not all = **3pt**; leaving blank = **0pt**. A total negative score in Exercise 1 counts as 0pt in the rest of the exam.

1.1) Mark those formulas below that are equivalent to  $p \vee q \rightarrow r$  in classical propositional logic:

- ☐  $(p \rightarrow r) \wedge (q \rightarrow r)$
- ☐  $(p \rightarrow r) \vee (q \rightarrow r)$
- ☐  $\neg r \rightarrow \neg p \wedge \neg q$
- ☐  $\neg(p \wedge q \wedge \neg r)$

1.2) The logic program  $P$  with rules  $\boxed{a \text{ :- not } c. \quad a \text{ :- } b \quad c \text{ :- } b}$  is stratified. Mark the rules below that, if they were (individually) added to  $P$ , they would make the result a non-stratified program.

- |   |   |
|---|---|
| <input type="checkbox"/> $\boxed{c \text{ :- } a.}$     | <input type="checkbox"/> $\boxed{b \text{ :- } a.}$     |
| <input type="checkbox"/> $\boxed{p \text{ :- not } p.}$ | <input type="checkbox"/> $\boxed{b \text{ :- not } a.}$ |

1.3) Given the following logic program  $\boxed{p \text{ :- } q. \quad p \text{ :- not } r. \quad r \text{ :- } p, \text{not } q}$

- ☐ the reduct with respect to  $\{q\}$  is the program  $\boxed{p \text{ :- } q. \quad p \text{ :- not } r.}$
- ☐ the reduct with respect to  $\emptyset$  is the program  $\boxed{p \text{ :- } q. \quad p. \quad r \text{ :- } p.}$
- ☐ the reduct with respect to  $\{r\}$  is the program  $\boxed{p \text{ :- } q. \quad r \text{ :- } p.}$
- ☐ the reduct with respect to  $\{p, q\}$  is the program  $\boxed{\quad}$
- ☐ the reduct with respect to  $\{q\}$  is the program  $\boxed{p \text{ :- } q. \quad p.}$

1.4) The rule  $\boxed{p \text{ :- not } r.}$  used above corresponds to the implication  $\neg r \rightarrow p$  that is equivalent to  $p \vee r$  in classical logic, but is strictly *stronger* in the logic of Here-and-There (HT). Mark those HT interpretations that are HT models of  $\neg r \rightarrow p$  but not of  $p \vee r$ .

- ☐  $H = \{p\}, T = \{p\}$
- ☐  $H = \emptyset, T = \emptyset$
- ☐  $H = \{r\}, T = \{p, r\}$
- ☐  $H = \emptyset, T = \{r\}$

**Exercise 2 (10pt).** Write an ASP program that generates all ways to place 4 bishops in a chessboard so that they do not attack each other. Use predicate `bishop(X,Y)` meaning there is a bishop at row `X` and column `Y`. (NOTE: in chess, bishops attack other pieces in the same diagonal).

```
#const n=8.  
cell(1..n,1..n).
```

```
#show bishop/2.
```

**Exercise 3 (8pt).** The following `telingo` program tries to move a robot in a grid from an initial position at (0,0) to a goal position at (3,4). Complete the program to fulfil the two missing requirements: (1) move the robot to some adjacent position (up, down, left or right); (2) the robot cannot step out of the grid.

```
#program initial.  
grid(0..3,0..4).  
wall(0,2). wall(2,2). wall(3,2). robot(0,0). goal(3,4).  
  
#program dynamic.  
% Move the robot to some adjacent position  
  
----- :- 'robot(X,Y).  
  
:- robot(X,Y), _wall(X,Y).      % Do not step into a wall  
  
% Do not step out of the grid  
  
-----  
  
#program final.  
:- robot(X,Y), not _goal(X,Y).  % Reach the goal at last state
```

**Exercise 4 (4pt).** Write a formula in Description Logic (DL) that describes the set of red (*Red*) cars (*Car*) that have some foreign (*Foreign*) owner (*owned\_by*).